

AI for Code-based Cryptography

SAC 2025

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Post-Quantum Cryptography Standards

NIST Standardization Process & Algorithm Selection

Category	Primary Algorithm	Alternate Algorithms
Public-Key Encryption/KEMs	CRYSTALS-Kyber	HQC
Digital Signatures	CRYSTALS-Dilithium	FALCON, SPHINCS+

Fourth Round KEM Finalists (2022-2025)

• BIKE

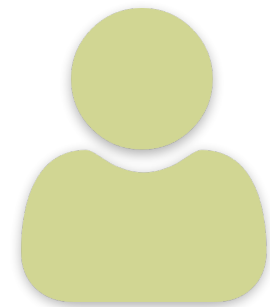
• Classic McEliece

• HQC (*selected as alternate in March 2025*)

• SIKE (*withdrawn due to security concerns*)

Source: National Institute of Standards and Technology (NIST)

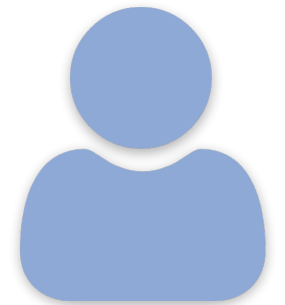
Classic McEliece



Alice

Bob's Public Key

$$\mathbf{G}_p \in \mathbb{F}_2^{k \times n}$$



Bob

Bob's Private Key

$$\Gamma = (g, \alpha)$$

plaintext

$$m \in \mathbb{F}_2^k$$



$$r = m\mathbf{G}_p + e$$

$$wt(e) \leq t$$

ciphertext

r



Decode

m

Binary Irreducible Goppa Codes

- A family of **error-correcting codes** defined over a finite field \mathbb{F}_q with **$q=2$** .

- **Parameterized by $\Gamma = (g, \alpha)$:**
 - ▶ A set of distinct elements $\alpha_1, \alpha_2, \dots, \alpha_n \in \mathbb{F}_{q^m}$ called the **support**.
 - ▶ A polynomial $g(x) \in \mathbb{F}_{q^m}[x]$ of degree t , **irreducible**.

● Key Properties

- Code dimension **$k \geq n - mt$**

✓ **Corrects up to t errors** in a codeword

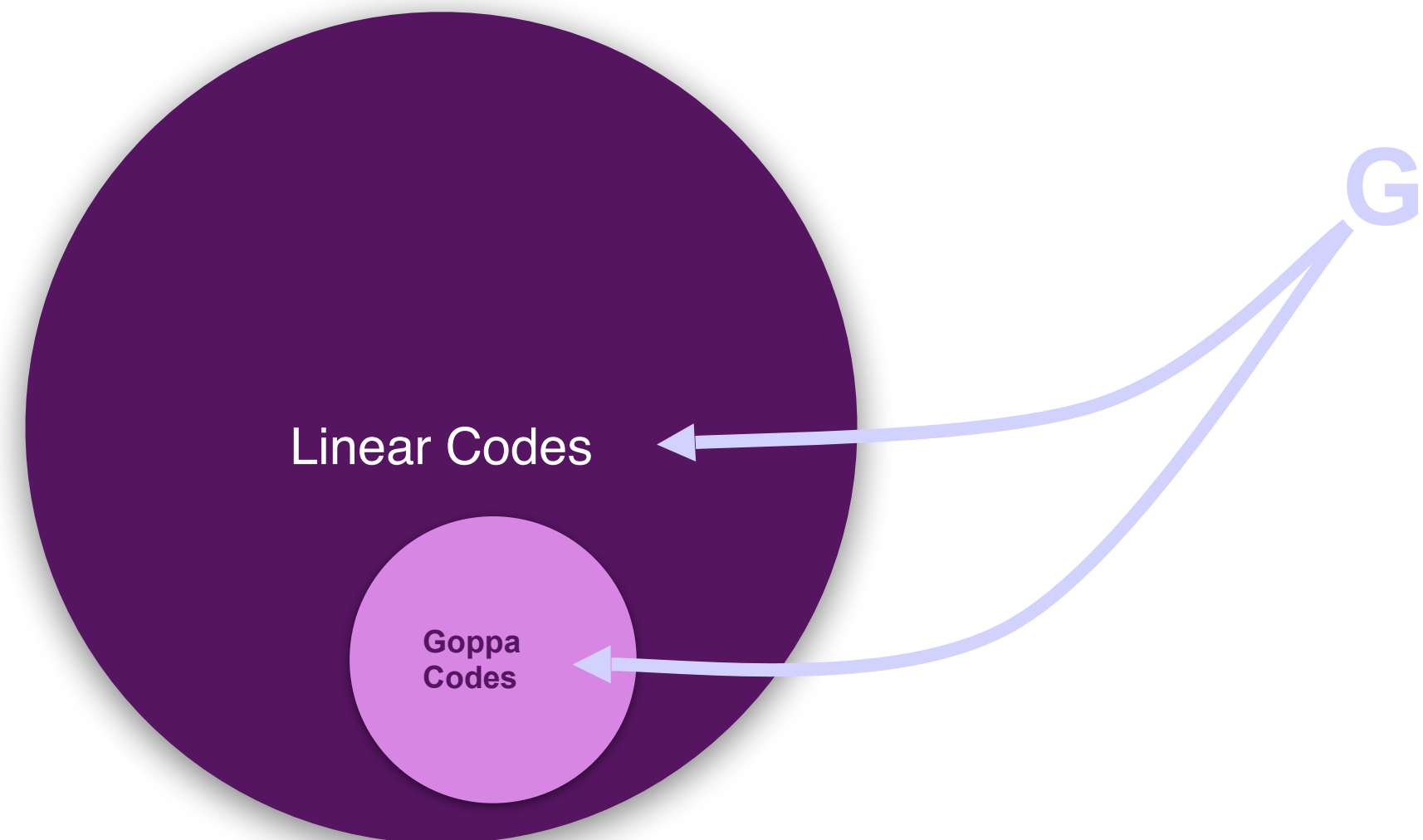
Defined as the \mathbb{F}_q -kernel of $V_t[\alpha, \beta]$

Where $\beta = (g(\alpha_1)^{-1}, g(\alpha_2)^{-1}, \dots, g(\alpha_n)^{-1})$

$$V_t[\alpha, \beta] = \begin{pmatrix} \beta_1 & \beta_2 & \cdots & \beta_n \\ \beta_1\alpha_1 & \beta_2\alpha_2 & \cdots & \beta_n\alpha_n \\ \vdots & \vdots & \ddots & \vdots \\ \beta_1\alpha_1^{t-1} & \beta_2\alpha_2^{t-1} & \cdots & \beta_n\alpha_n^{t-1} \end{pmatrix}$$

Security Analysis of McEliece

- Hardness of Decoding
- Goppa Distinguishing Problem



Some Distinguishers in the Literature



J.-C. Faugère, V. Gauthier-Umana, A. Otmani, L. Perret, J.-P. Tillich.
A Distinguisher for High Rate McEliece Cryptosystems.
IEEE-IT 2013



A. Couvreur, R. Mora, J.-P. Tillich.
A New Approach Based on Quadratic Forms to Attack the McEliece Cryptosystem.
Asiacrypt 2023.



H. Randriambololona.
The Syzygy Distinguisher.
EUROCRYPT 2025.

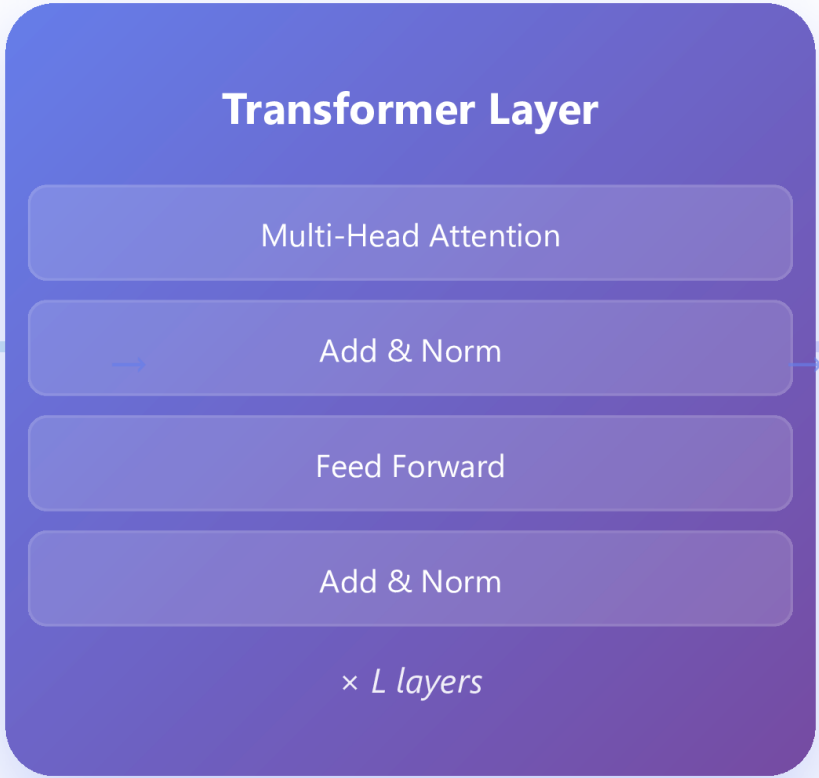
Transformer-Based Binary Classification

G

Input Tokens

- g_1
- g_2
- g_3
- g_4
- \vdots
- g_n

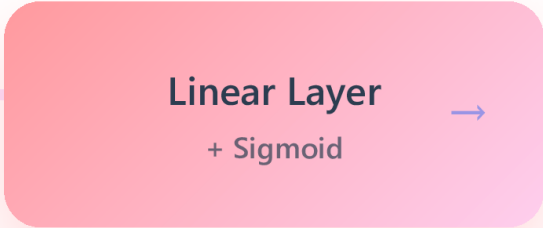
Encoder Stack



Aggregation



Classification



Output

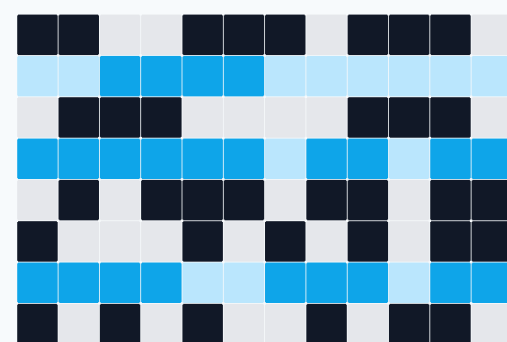
- ✓ Class 1
 $P(y = 1)$
- ✗ Class 0
 $P(y = 0)$

Tokenizing & Encoding Binary Matrices for Transformers

■ bit = 1 ■ bit = 0 — flow

Rows → Tokens

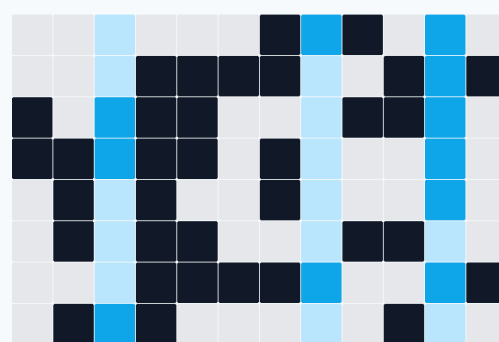
Each matrix row is a token; $\text{Linear}(m \rightarrow d)$



row tokens

Columns → Tokens

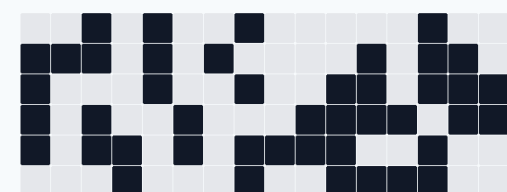
Each column is a token; $\text{Linear}(n \rightarrow d)$



column tokens

Flattened Bits

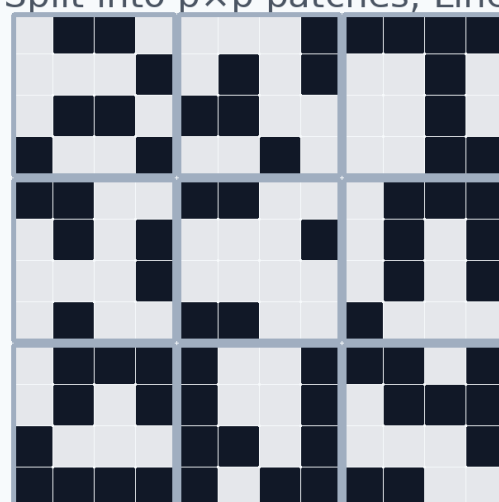
Flatten to a 1D bit stream; $\text{Embedding}(2 \rightarrow d)$ or $\text{Linear}(k\text{-bit} \rightarrow d)$



bit or n-gram tokens

2D Patch Embeddings

Split into $p \times p$ patches; $\text{Linear}(p^2 \rightarrow d)$



patch tokens

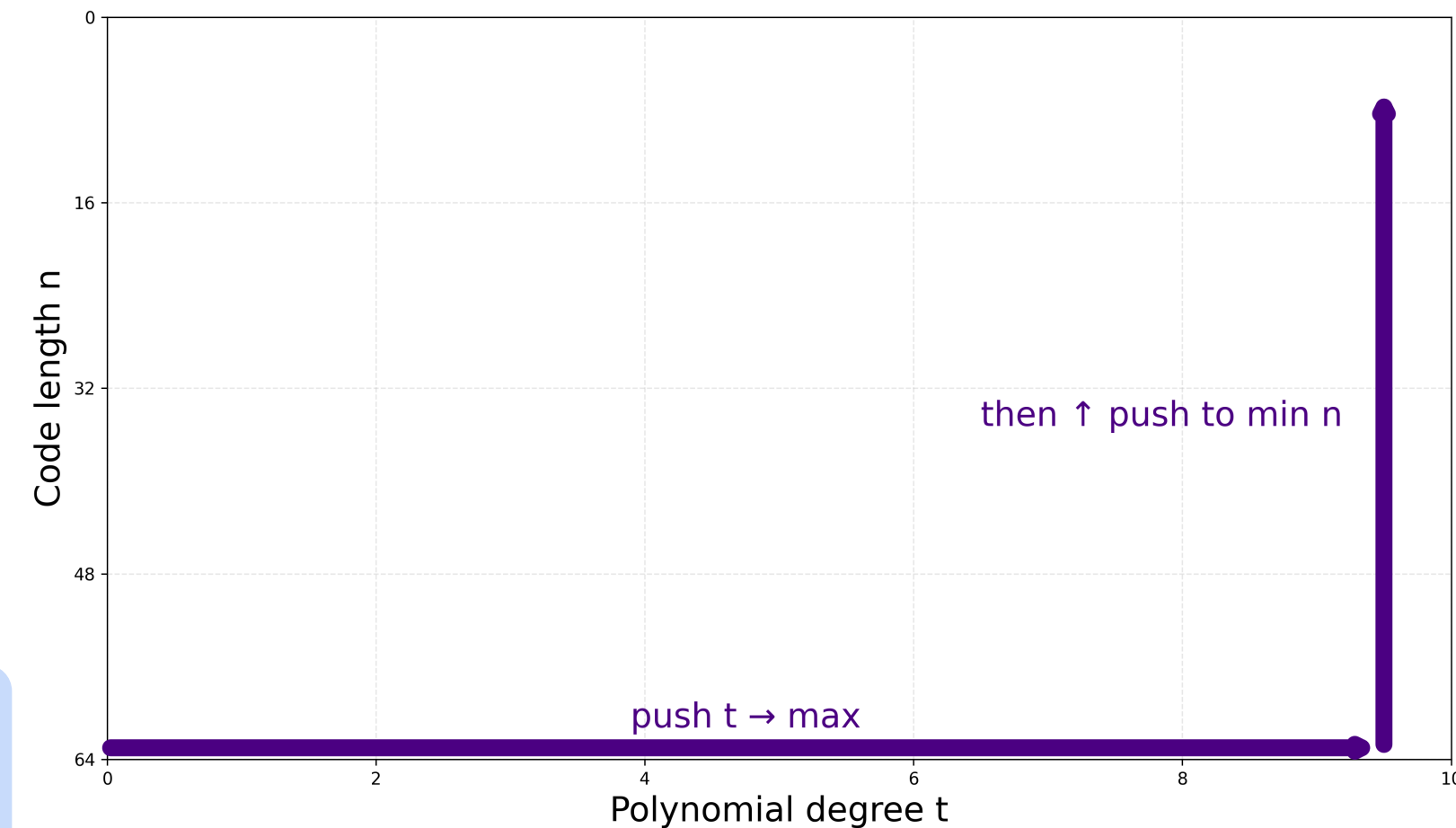
Evaluation of the distinguishers in the literature

[Randriam 24 & CMT 23]

Consider a field extension degree m
(e.g. $m=6$)

For maximum $n = q^m$ (e.g. $n=64$),
determine maximal distinguishable
degree t .

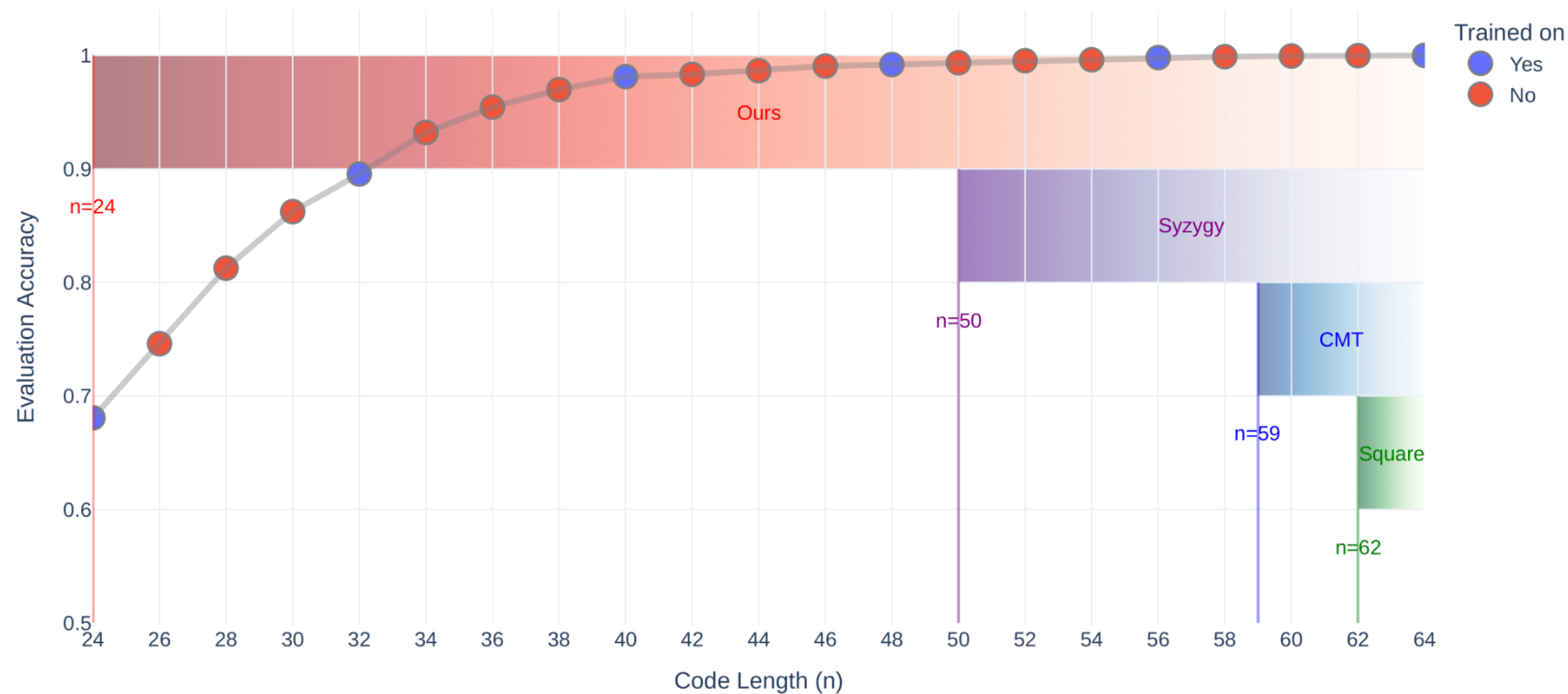
Fix t , determine minimal
distinguishable n .



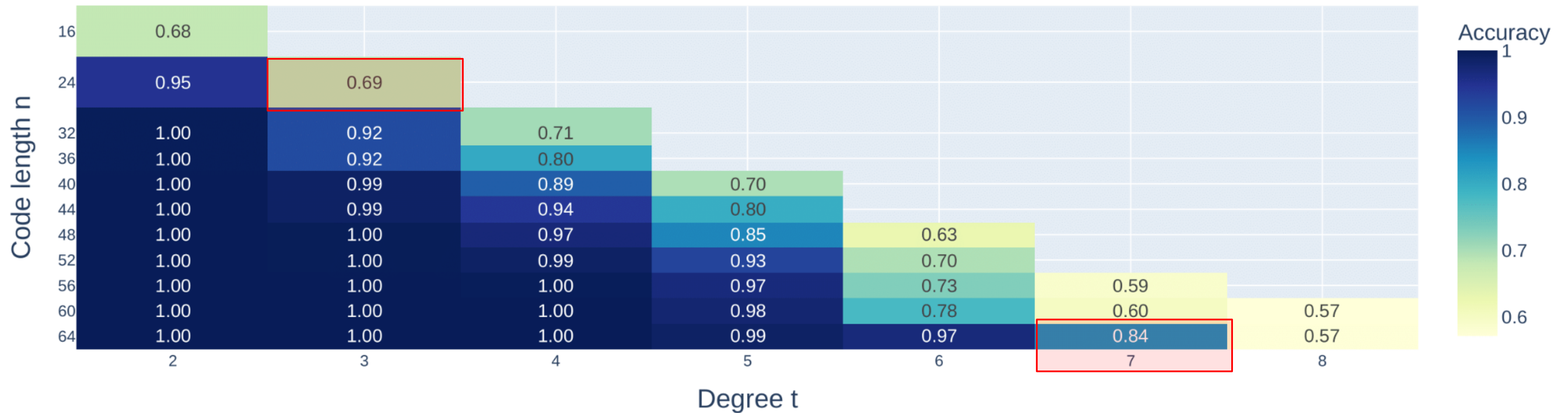


Results:

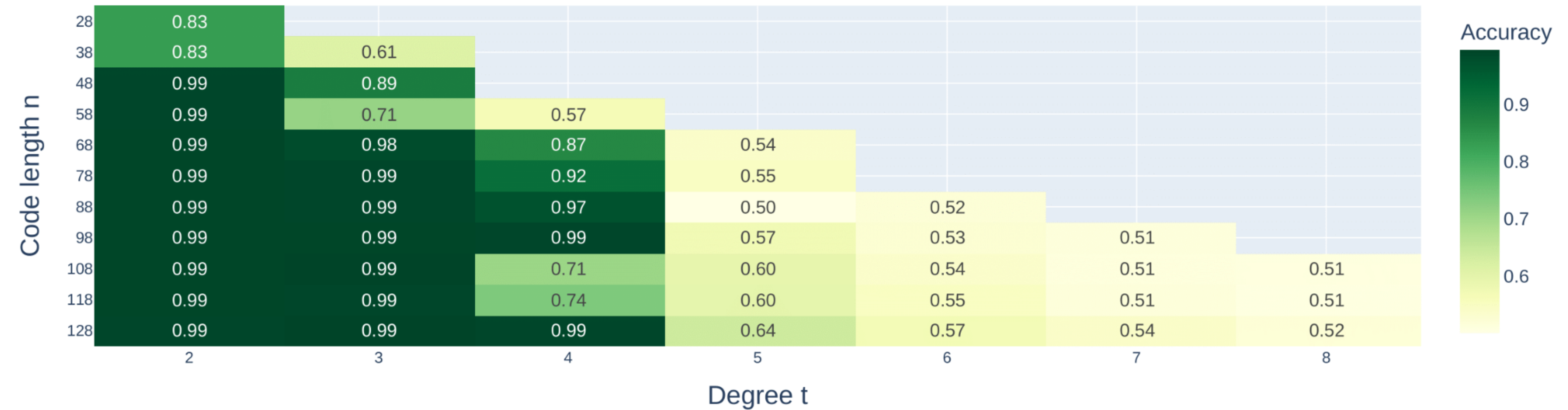
- Model accuracy as a function of code length. The model is trained on Binary Goppa Codes with $m=6$ and $t=3$.
- Scatter points indicate the evaluation accuracy of our model.
- The scatter color indicates the range where the model was trained ($n = 24 + 8k$ for $k=0,1,\dots$)



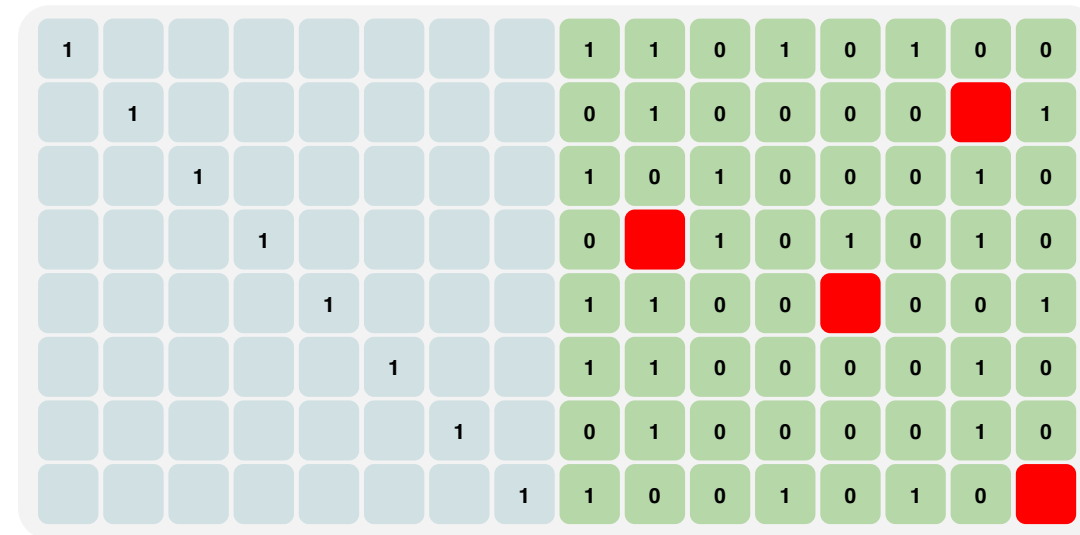
- Heatmap of model accuracy for $q=2$, $m=6$ as a function of code length n and degree parameter t .



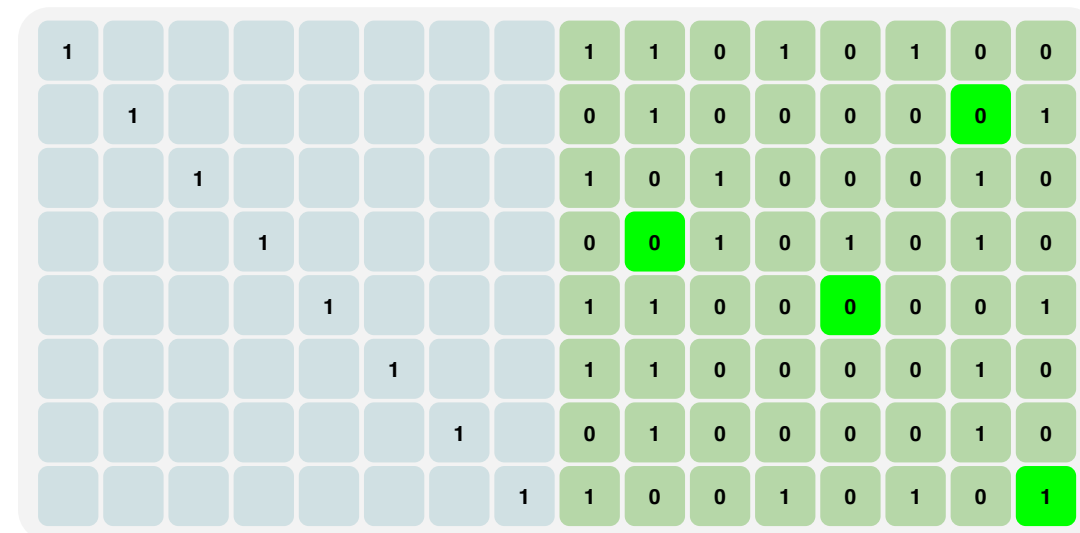
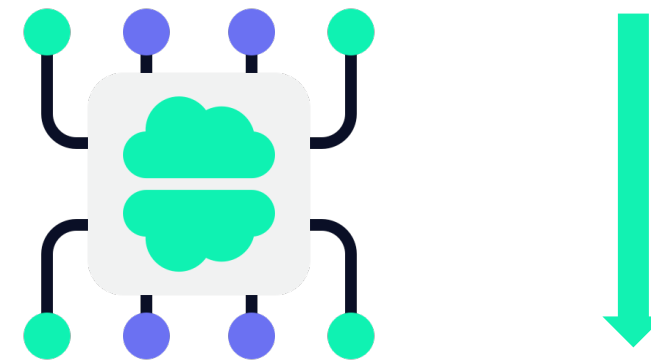
Heatmap of model accuracy for $q=2$, $m=7$ as a function of code length n and degree parameter t .



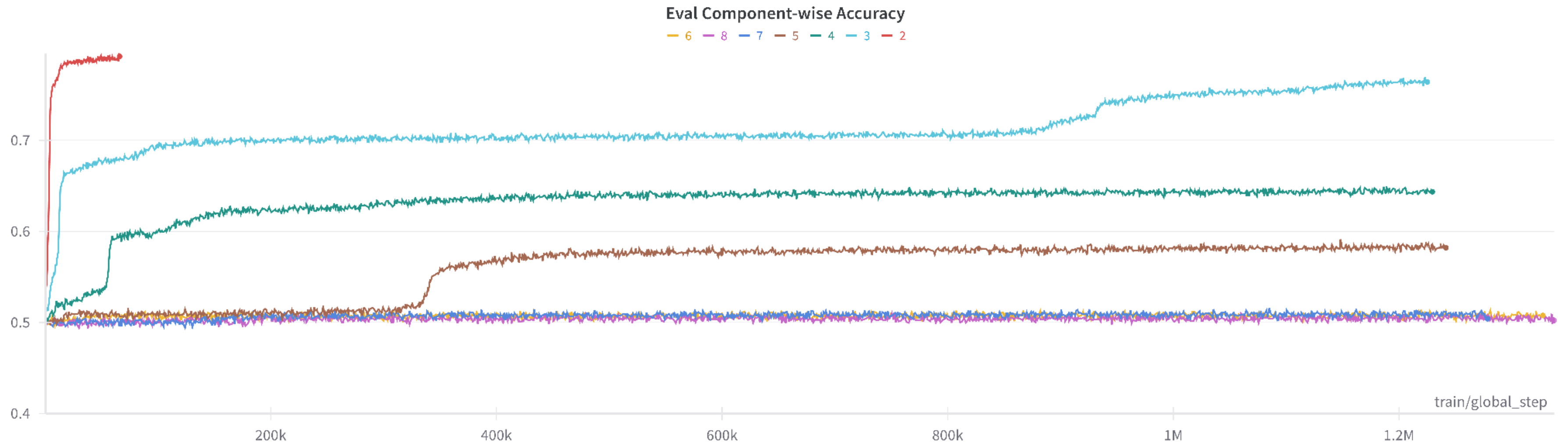
Can we do better than just distinguish ?



Training on a new task:
Goppa Code Completion



Test Accuracy on n=64, m=6





Summary and Conclusion

Paper:



Mohamed Malhou, Ludovic Perret, Kristin Lauter

AI for Code-based Cryptography

Code available at github.com/facebookresearch/ai4code-cryptanalysis

- ★ Improve SOTA Goppa distinguishers in toy examples.
 - What are the limits of this approach and how to estimate the complexity?
- ★ Results can be extended to (QC) MDPC Codes (BIKE).